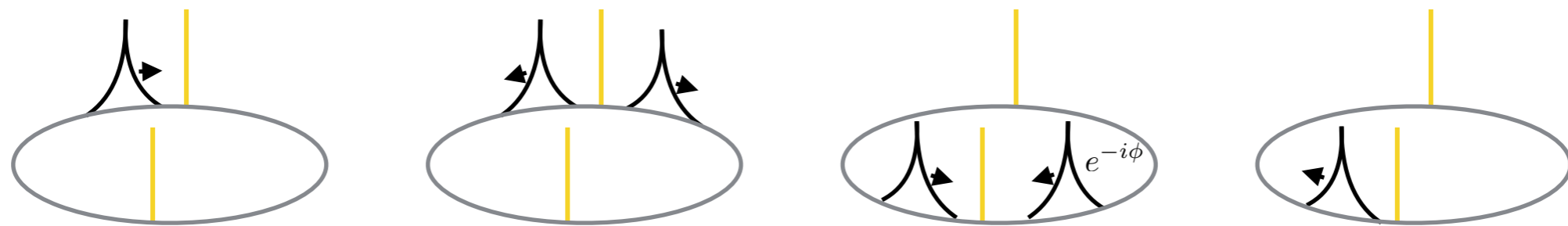


Soliton interferometry in atomtronic circuits.



Piero Naldesi

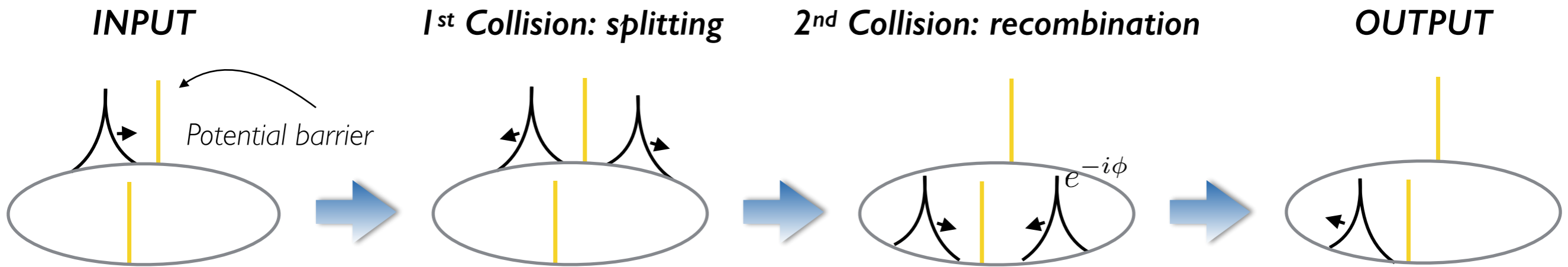
LPMMC - Laboratoire de Physique et
Modélisation des Milieux Condensés

Grenoble



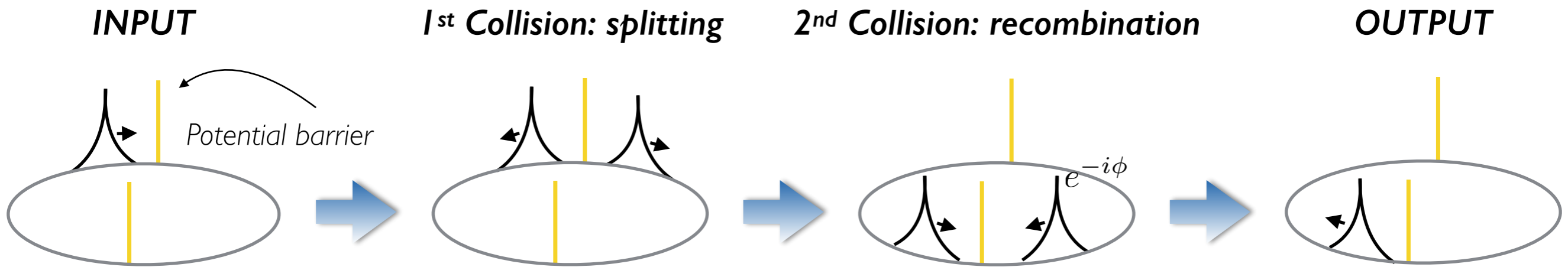
● **Introduction - Solitons Interferometry in ATOMTRONIC circuits**

Mach-Zehnder interferometer with solitons

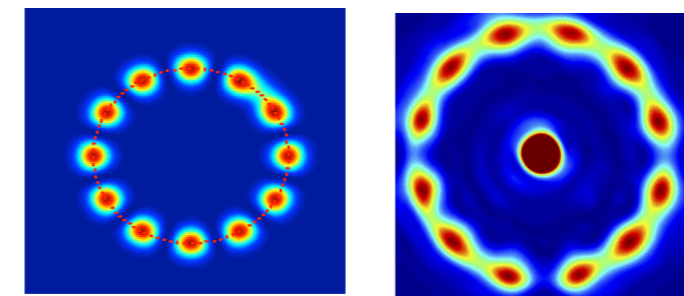
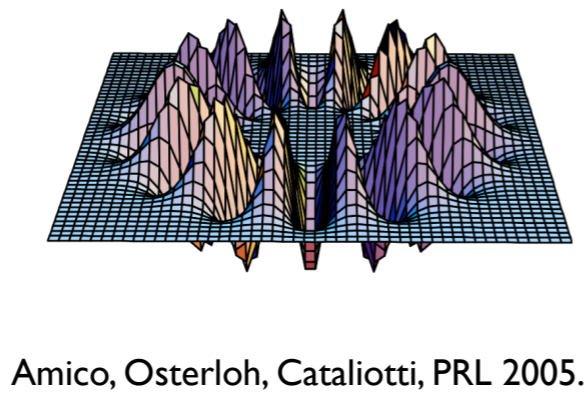


● **Introduction - Solitons Interferometry in ATOMTRONIC circuits**

Mach-Zehnder interferometer with solitons



Atomtronic devices provide the best framework for experiments with ultra-cold gases in a ring geometry



Ring-shaped optical lattices

Amico, Aghamalyan, Aukstol, Crepatz, Kwek, Dumke SREP 2014.

Aghamalyan, Nguyen, Aukstol, Gan, Martinez Valado, Condylys, Kwek, Dumke, Amico NJP 2016

Aghamalyan, Cominotti, Rizzi, Rossini, Hekking, Minguzzi, Kwek, Amico, NJP 2015.

• *Bosons with attractive interaction in a lattice - Bose-Hubbard Model*

$$\hat{H}(U) = -J \sum_{j=-L/2}^{L/2} \left(b_j^\dagger b_{j+1} + b_{j+1}^\dagger b_j \right) + \frac{U}{2} \sum_{j=-L/2}^{L/2} \hat{n}_j (\hat{n}_j - 1)$$

attractive
interactions
 $U < 0$

N-particles problem
is not exactly
solvable: still a lot of
open questions!

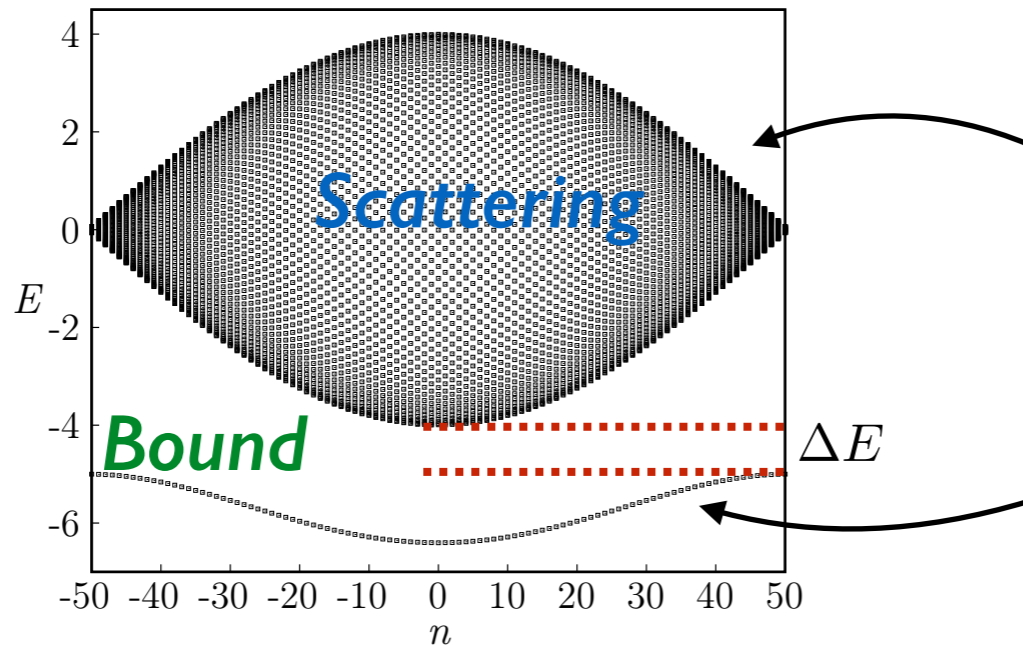
Bosons with attractive interaction in a lattice - Bose-Hubbard Model

$$\hat{H}(U) = -J \sum_{j=-L/2}^{L/2} \left(b_j^\dagger b_{j+1} + b_{j+1}^\dagger b_j \right) + \frac{U}{2} \sum_{j=-L/2}^{L/2} \hat{n}_j (\hat{n}_j - 1)$$

attractive interactions
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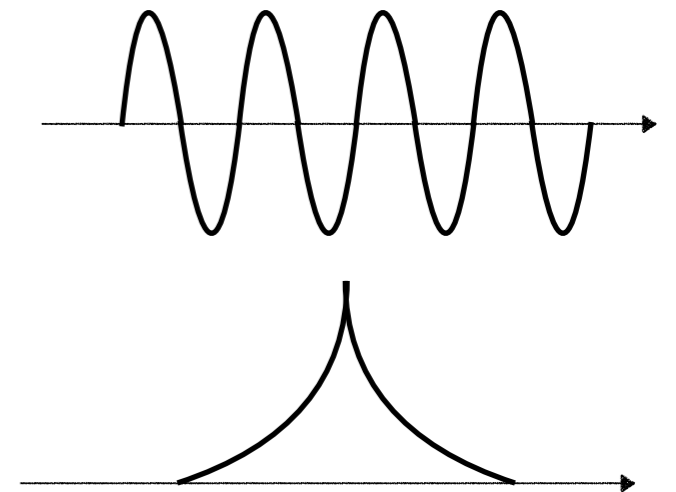
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2-particle problem (exactly solvable)



Scattering states

Bound states



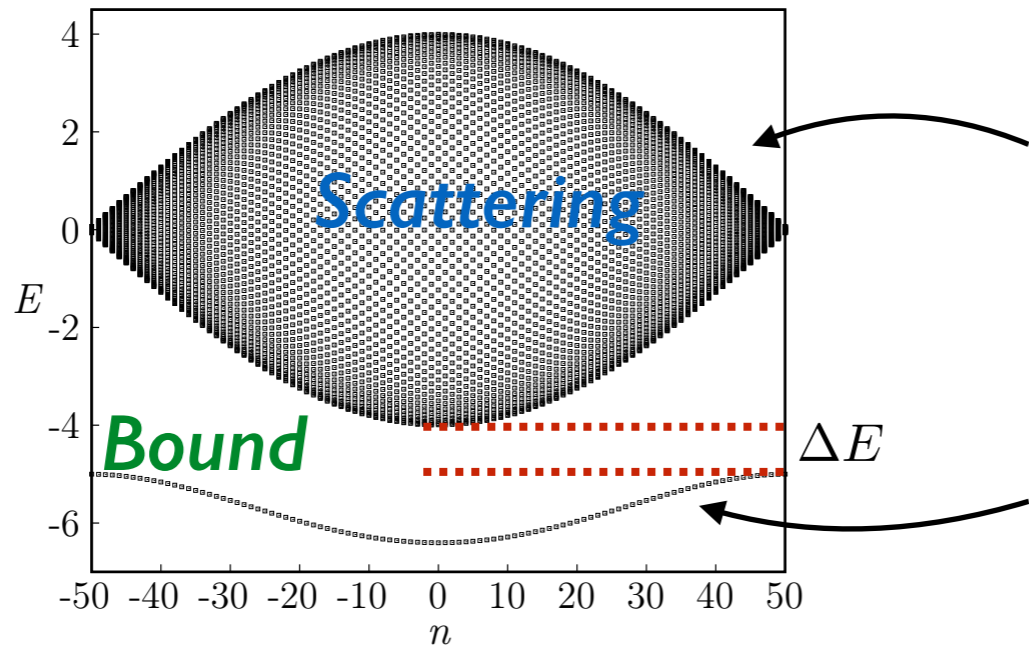
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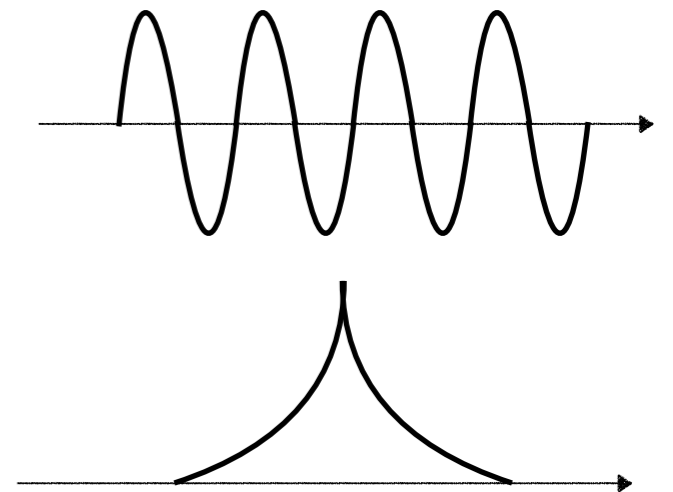
attractive interactions
 $U < 0$

N-particles problem is not exactly solvable: still a lot of open questions!

2-particle problem (exactly solvable)



Scattering states



Bound states

DMRG: Density Matrix Renormalization Group

S. R. White, PRL 69 2863 (1992) S. R. White, PRB 48 10345 (1993) A. Feiguin, S. R. White, PRB, 72, 020404 (2005)

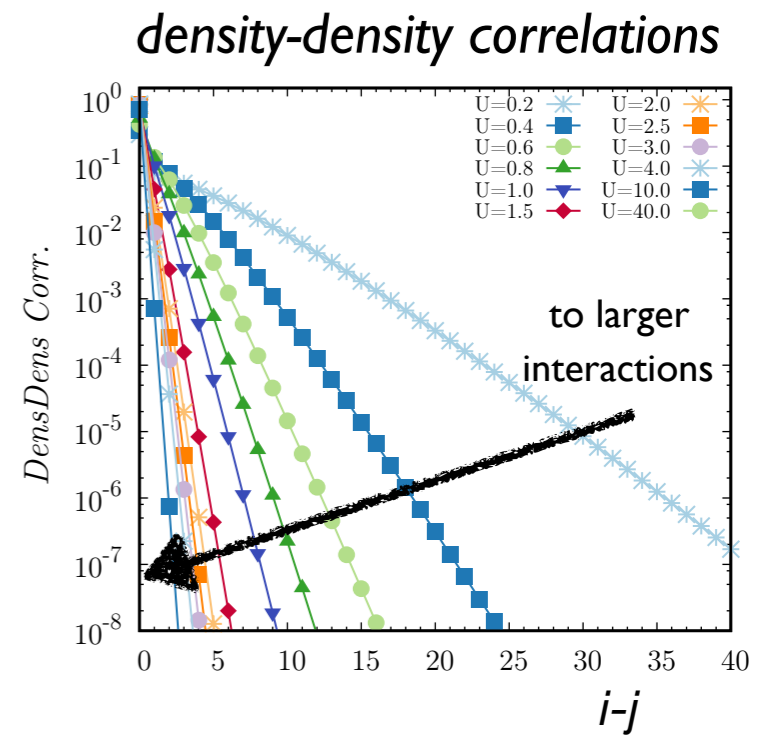
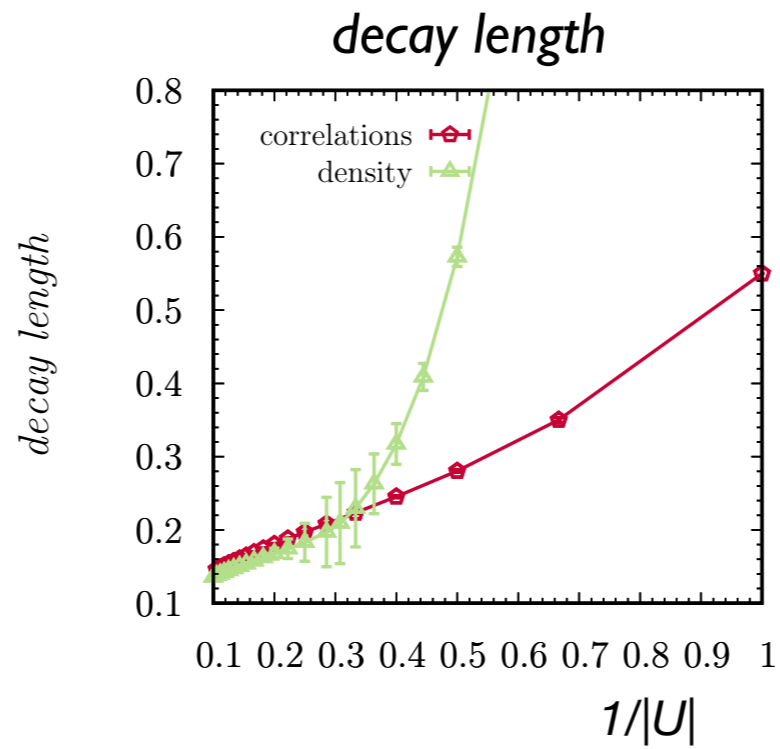
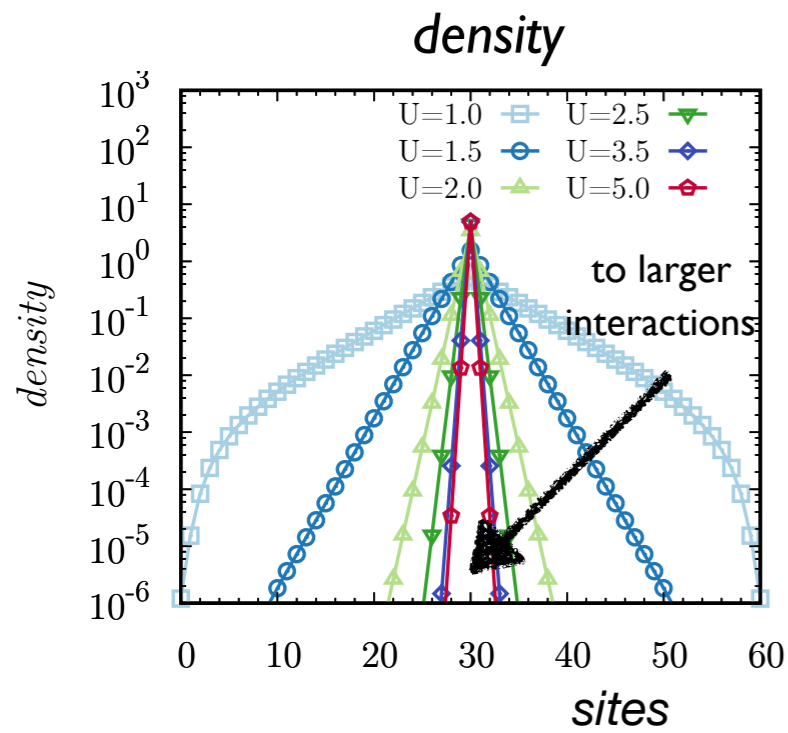
Numerical technique for ground state and firsts excited states in lattice systems.



IDEA: describe the system with only the most relevant states in the density matrix

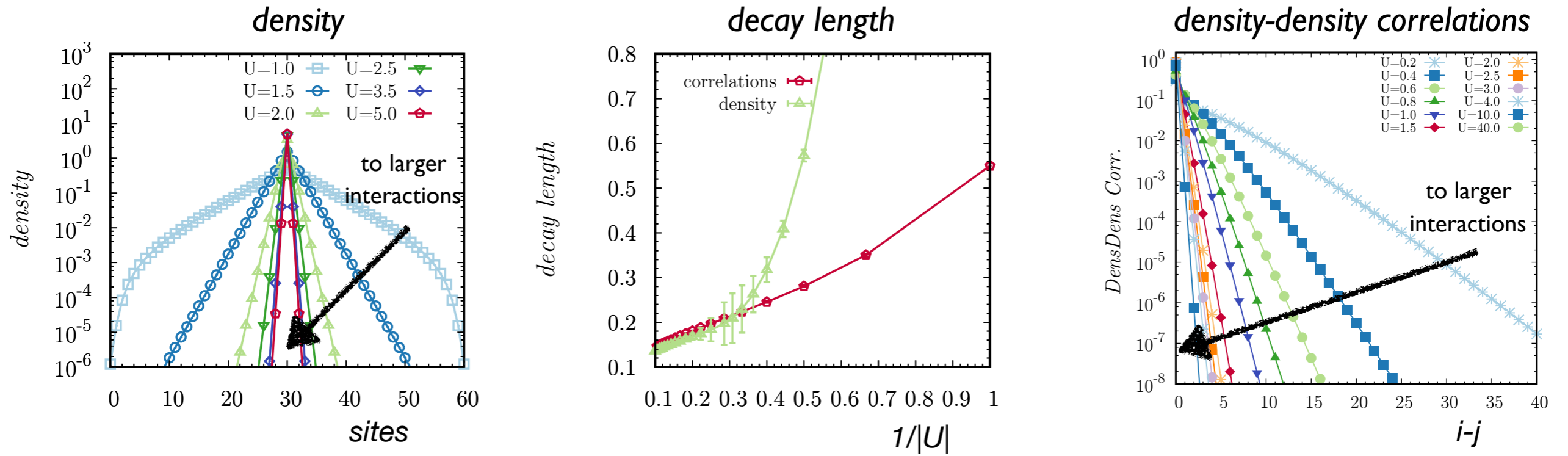
Results: density, correlations & fragmentation

Characterisation of solitons from the decay of density and density-density correlations.

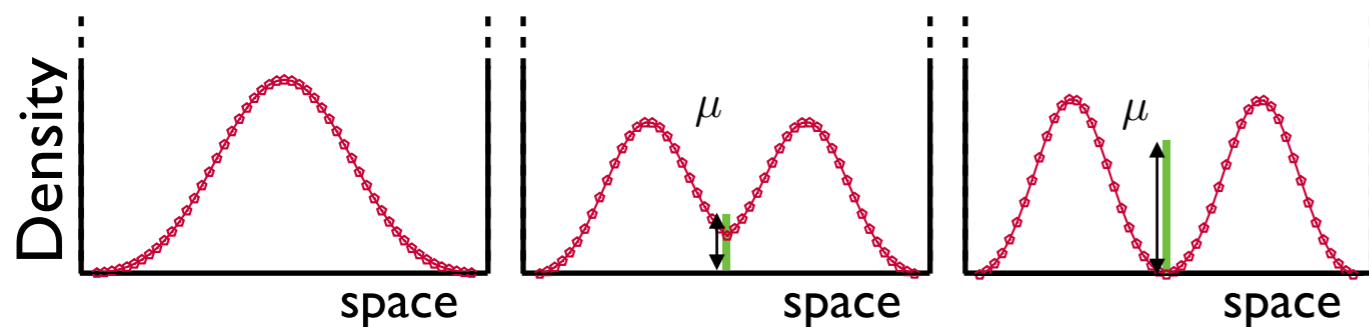


Results: density, correlations & fragmentation

Characterisation of solitons from the decay of density and density-density correlations.



Splitting of a soliton in a fragmented state by a potential barrier.



$$|\psi\rangle = \sum_{\alpha=0}^N c_{\alpha} |N-\alpha\rangle_L |\alpha\rangle_R$$

