Ultracold atoms under an artifical gauge field : persistent currents

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Frank Hekking Memorial Workshop







Funding from ANR SuperRing

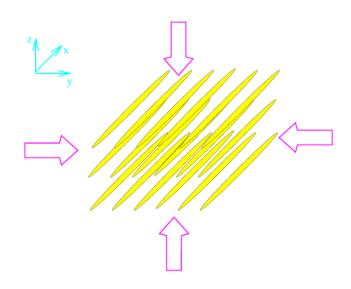
One-dimensional quantum systems with ultracold atoms

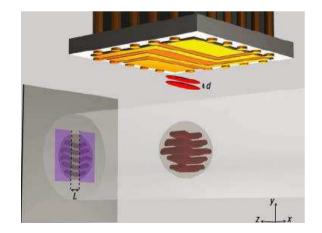
- Cylindrical geometry
- Very large transverse confinement

 All energy scales smaller than transverse energy

 $\mu, k_B T \ll \hbar \omega_\perp$

Realization : 2D optical lattices or chip traps





Interactions in 1D quantum gases

 Interactions due to atomatom collisions

(short range, s-wave scattering length)

• Effective 1D interactions

$$v(x) = g\delta(x)$$

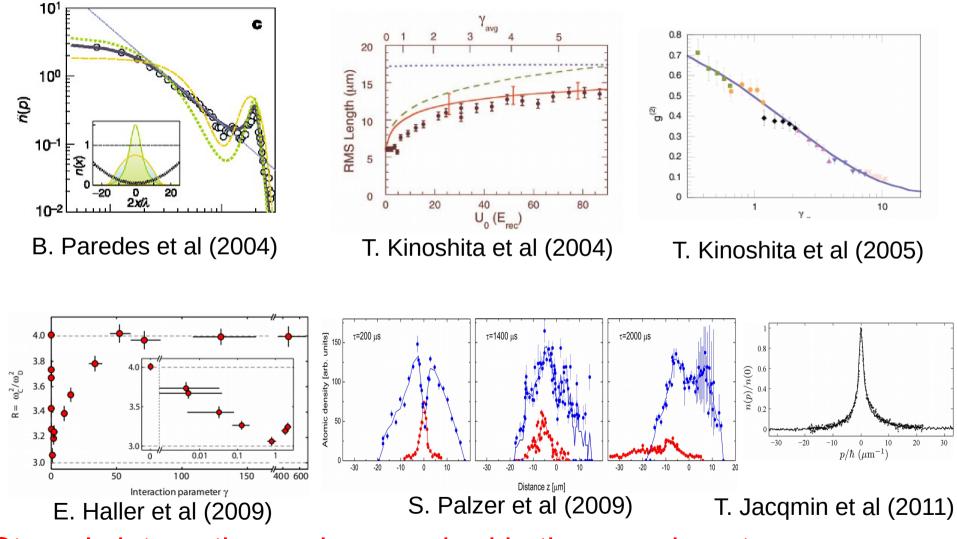
• Hamiltonian (Lieb-Liniger model with external potential)

$$\mathcal{H} = \sum_{i} -\frac{\hbar^2}{2m} \frac{\partial^2}{\partial x_i^2} + V(x_i) + g \sum_{i < j} \delta(x_i - x_j)$$

• Dimensionless interaction strength :

$$\gamma = gn/(\hbar^2 n^2/m)$$

One-dimensional quantum gases : experiments



Strongly interacting regime reached in the experiment

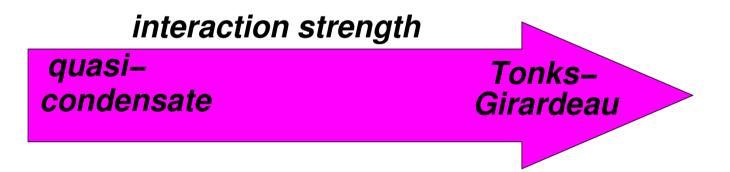
Line diagram for 1D bosons

• Weak interactions:

a condensate with fluctuating phase

• Strong interactions:

fermionization

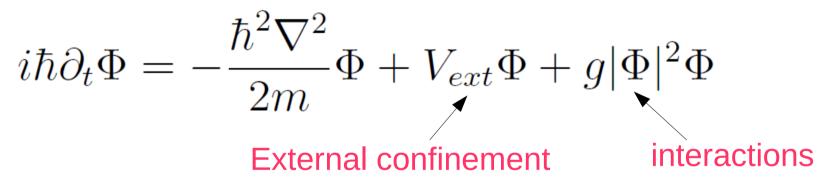


- No phase transition in uniform wires
- But very different behaviour from weak to strong interactions

The weakly interacting regime : Gross-Pitaevskii equation

• Mean-field description of a Bose gas

with 'condensate wavefunction' $\Phi(x, t)$



- Nonlinear Schroedinger equation: superfluidity, solitons...
- Even in the dilute regime $E_{int} \ll E_{kin}$, under external confinement/disorder the interactions are important [Baym-Pethick, Stringari]

Intermediate interactions : bosonizing the bosons with Luttinger liquid theory

Quantum hydrodynamics, low-energy theory

for the superfluid phase ϕ

and the density fluctuation $\partial_x \theta$

$$\mathcal{H} = \frac{\hbar v_s}{2\pi} \int dx K (\partial_x \phi)^2 + \frac{1}{K} (\partial_x \theta)^2$$

- Sound velocity and Luttinger parameter (compressibility) from the microscopic theory
- Phonon excitation spectrum: valid at intermediate and large interactions

Strong interactions : the Tonks-Girardeau gas

- Infinitely strong repulsions mimick Pauli principle
- Exact solution [Girardeau, 1960] mapping onto a Fermi gas

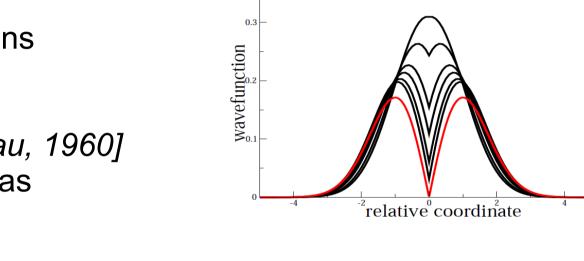
$$\Psi_B(x_1, ..., x_N) = \mathcal{A} \det[\phi_j(x_\ell)]$$

with

$$\mathcal{A} = \prod_{1 \le j \le \ell \le N} \operatorname{sign}(x_j - x_\ell)$$

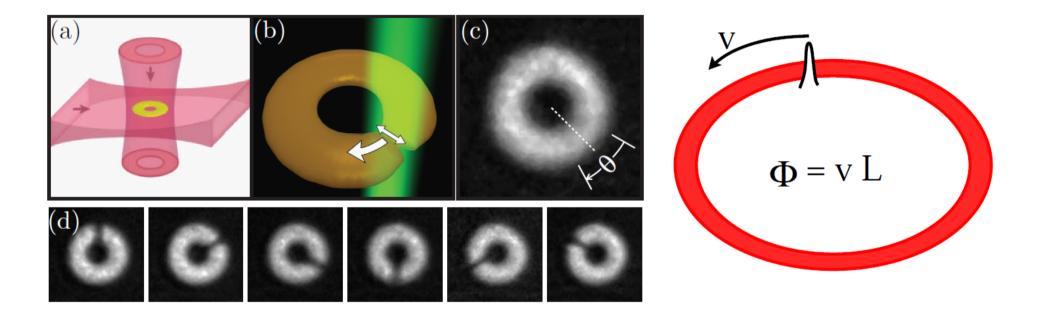


- inhomogeneous systems
- finite-temperature properties
- out-of-equilibrium dynamics



No length scale associated to interactions : scale invariance

Strongly interacting bosons on a ring under a gauge field

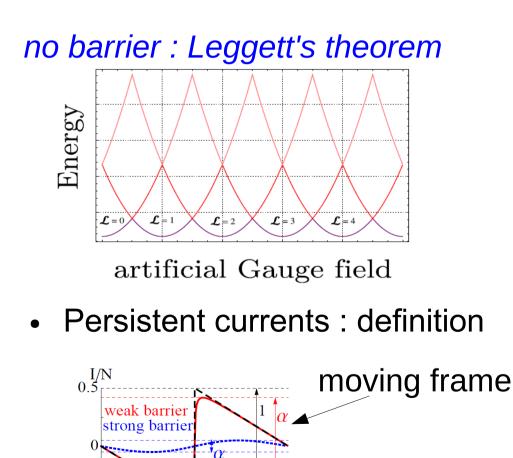


 Barrier rotation : a way to create an artificial gauge field for neutral atoms

$$\mathcal{H} = \frac{1}{2m} \left(p - A \right)^2 + V_{ext} + U_{int}$$

Persistent currents

- Ground state energy in presence of gauge field ?
 - \rightarrow periodicity of energy levels



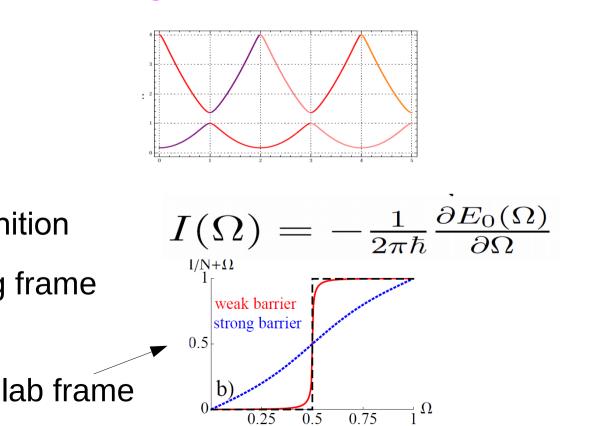
a

0.5

0.75

-0.5

with barrier : coherent mixing of angular momentum states



Exact results at zero and infinite interactions

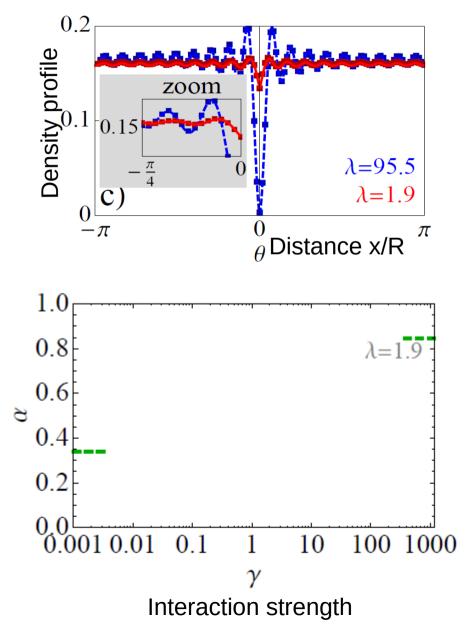
 Density profiles along the ring : Friedel oscillations at strong interactions

a signature of the strongly correlated regime

Amplitude of persistent currents : at large interactions, effective barrier

$$U_{eff} = U_0/N$$





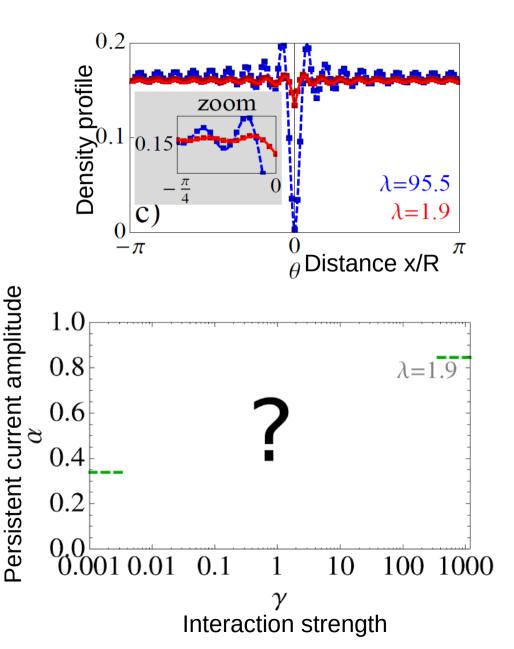
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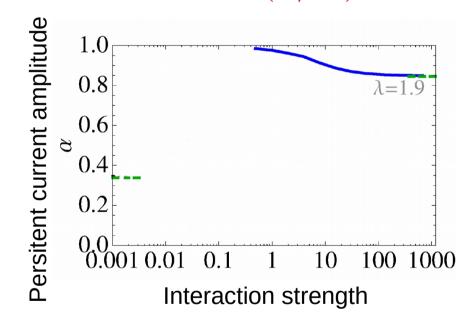
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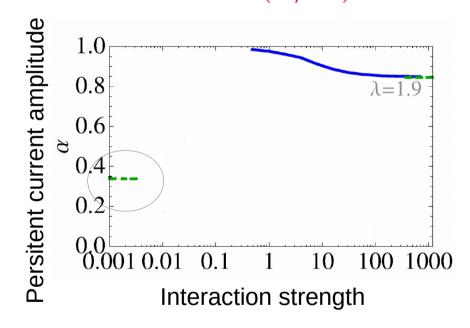
Strongly interacting limit

- Luttinger liquid theory : quantum fluctuations renormalize the barrier strength $U_{\rm eff} = U_0 (d/L)^K$



Strongly interacting limit

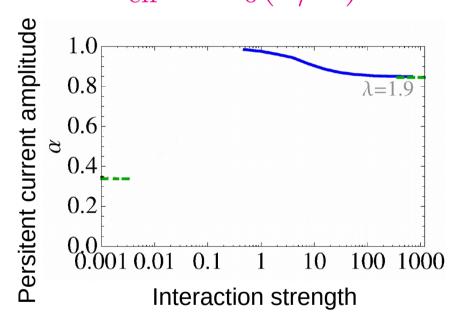
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??? Wrong trend ???

Strongly interacting limit

- Luttinger liquid theory : quantum fluctuations renormalize the barrier strength $U_{\rm eff} = U_0 (d/L)^K$



 At increasing interactions, density fluctuations renormalize the barrier less and less

- (duality) : phase fluctuations are more and more important at increasing interactions

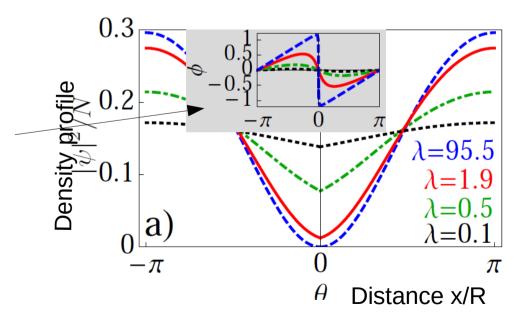
Weakly interacting limit

Neglect quantum fluctuations : Gross-Pitaevskii equation

$$\frac{\hbar^2}{2m} \left(-i\frac{\partial}{\partial x} + \frac{2\pi}{L}\Omega \right)^2 \Phi + U_0 \delta(x) \Phi + g |\Phi|^2 \Phi = \mu \Phi$$

(new soliton solution with Jacobi elliptic functions)

- The soliton is pinned by the barrier \rightarrow ground state
- Phase slips at the position of the barrier



Weakly interacting limit

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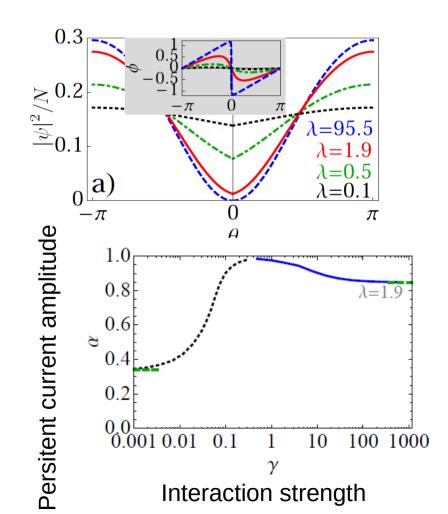
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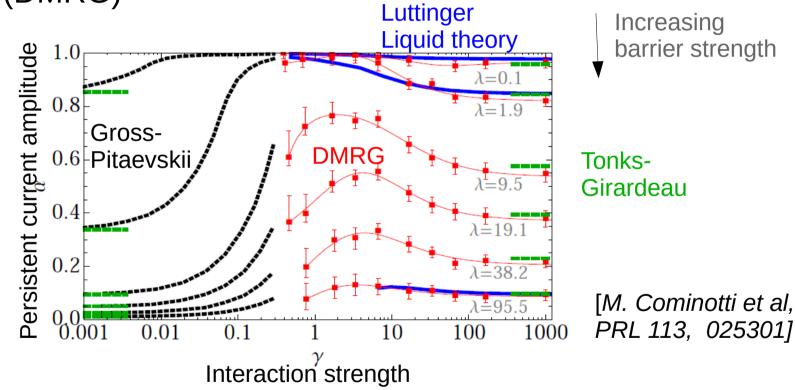
Optimal persistent current at intermediate interactions :

competition of classical screening and quantum fluctuations



Arbitrary interactions and barrier strengths

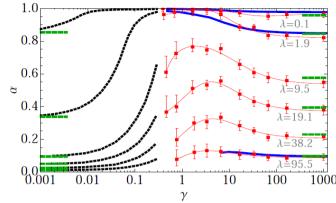
Persistent current amplitude : all the analytical results + numerical (DMRG)



 Interactions can turn a strong barrier into a weak one → quantum state manipulation, transport across a barrier, analog of Hawking effect, ...

Conclusions and perspectives

Non-monotonous behaviour of persistent currents for bosons on a ring : competition of classical screening and barrier renormalisation [Cominotti et al, PRL 2014]



Seminal idea on barrier renormalisation : Talk by Roberta Citro

Consequence of barrier renormalisation : dipole modes in a split trap [Cominotti et al, PRA 2015]

Applications for atomtronics : Talk by Luigi Amico

Beyond 1D rings : Poster by Nicolas Victorin

Dynamics of currents after a quench : Poster by Juan Polo

Atomtronics for bosons with attractive interactions : Poster by Piero Naldesi

Experiments with ultracold atoms on a ring : Talk by Hélène Perrin



Thank you Frank !!