

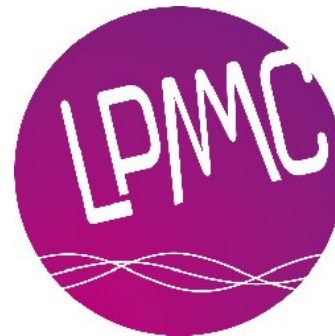
# Bosonic Lattice Double Ring Under A Gauge Field

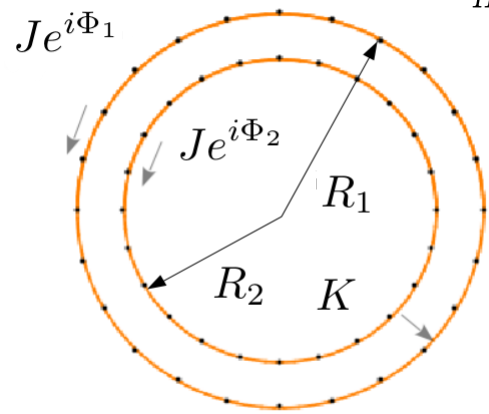
Nicolas Victorin

With

Frank Hekking and Anna Minguzzi

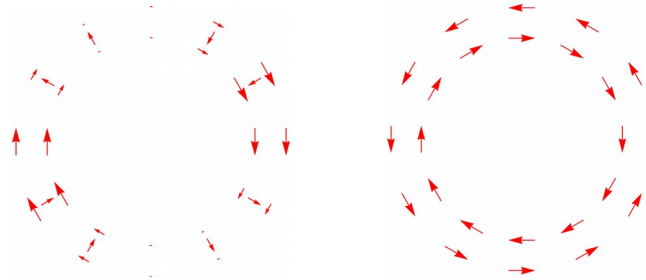
LPMMC-CNRS





$$\hat{H} = - \sum_{l=1,p=1,2}^{N_s} J_p \left( a_{l,p}^\dagger a_{l+1,p} e^{i\Phi_p} + a_{l+1,p}^\dagger a_{l,p} e^{-i\Phi_p} \right) - K \sum_{l=1}^{N_s} \left( a_{l,1}^\dagger a_{l,2} + a_{l,2}^\dagger a_{l,1} \right) + \frac{U}{2} \sum_{l=1,p=1,2}^{N_s} a_{l,p}^\dagger a_{l,p}^\dagger a_{l,p} a_{l,p}$$

$U = 0$  Two phases : Meissner and Vortex



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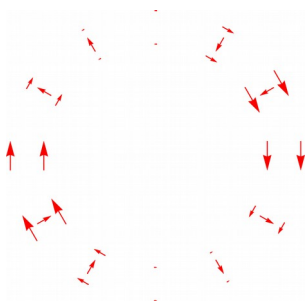
LPMCM-CNRS



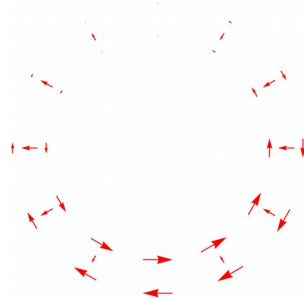
# Finite size effect

$$\Phi = \frac{\Phi_1 + \Phi_2}{2}$$

Number of vortices depends on the parity of the mean flux  $\Phi$

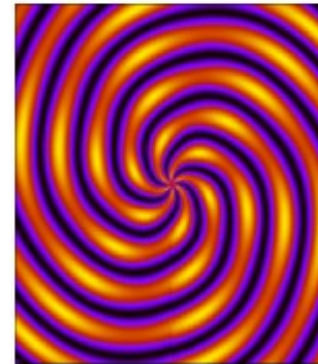


$\Phi$  Even

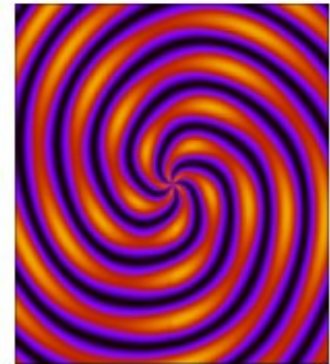


$\Phi$  Odd

Experimental way of seeing vortices

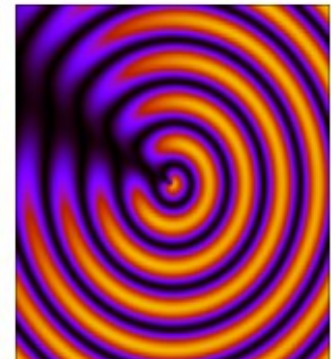


$\Phi$  Even



$\Phi$  Odd

Vortex phase



Meissner phase

# Mean field regime – New phases appear

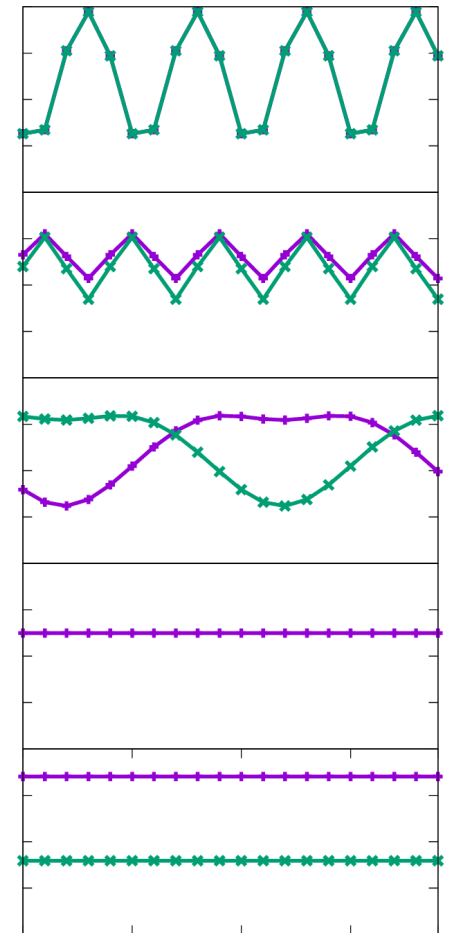
Discrete coupled non linear Schrödinger equations

$$i\partial_t \Psi_{l,1}(t) = -J\Psi_{l+1,1}(t)e^{i(\Phi+\phi/2)} - J\Psi_{l-1,1}(t)e^{-i(\Phi+\phi/2)} - K\Psi_{l,2}(t) + U|\Psi_{l,1}(t)|^2\Psi_{l,1}(t)$$

$$i\partial_t \Psi_{l,2}(t) = -J\Psi_{l+1,2}(t)e^{i(\Phi-\phi/2)} - J\Psi_{l-1,2}(t)e^{-i(\Phi-\phi/2)} - K\Psi_{l,1}(t) + U|\Psi_{l,2}(t)|^2\Psi_{l,2}(t)$$

→ We see new phases that break  $\mathbb{Z}_2$  and rotational symmetry of the system

$|\psi_{l,1}|^2/n$  —+—  
 $|\psi_{l,2}|^2/n$  —x—



Position