

# Quantum dynamics of a driven three-level Josephson-atom maser

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With: Nicolas Didier, Frank Hekking

Phys. Rev. B **82**, 214507 (2010)



# Completed work

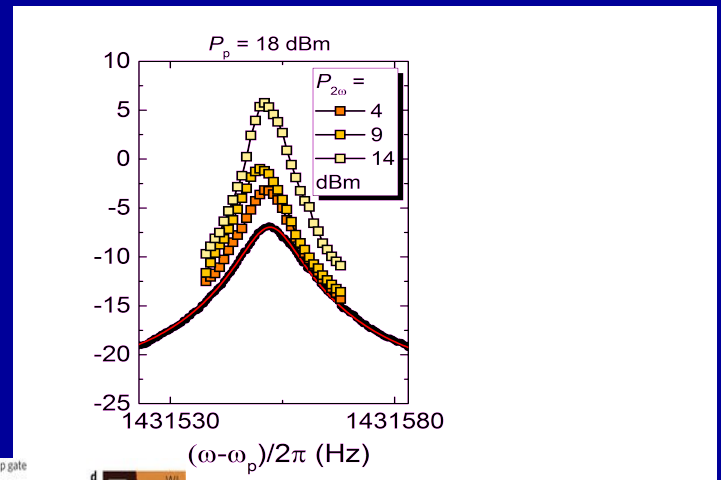
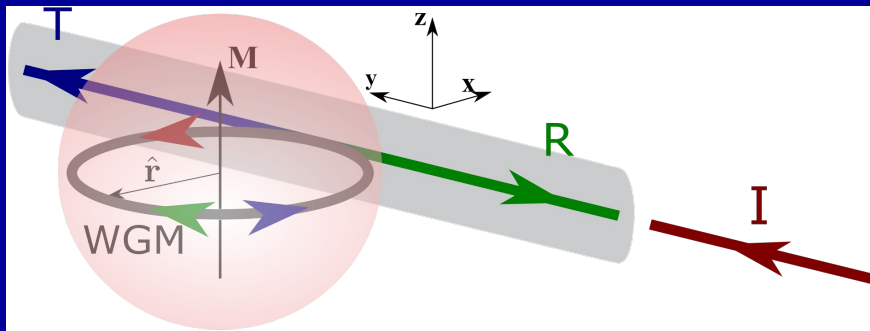
1. *Interaction Constants and Dynamic Conductance of a Gated Wire*  
Ya. M. Blanter, F. W. J. Hekking, and M. Büttiker,  
Phys. Rev. Lett. **81**, 1925 (1998)
2. *Supercurrent in long SFFS junctions with antiparallel domain configuration*  
Ya. M. Blanter and F. W. J. Hekking  
Phys. Rev. B **69**, 024525 (2004)
3. *Quantum dynamics of a driven three-level Josephson-atom laser*  
N. Didier, Ya. M. Blanter, and F. W. J. Hekking  
Phys. Rev. B **82**, 214507 (2010)

# Not completed work

- Extension of Blanter – Hekking – Büttiker to the wire with a barrier
- Self-consistent theory of radiation of a Josephson junction
- Nanomechanical cooling using superconductors
- ...

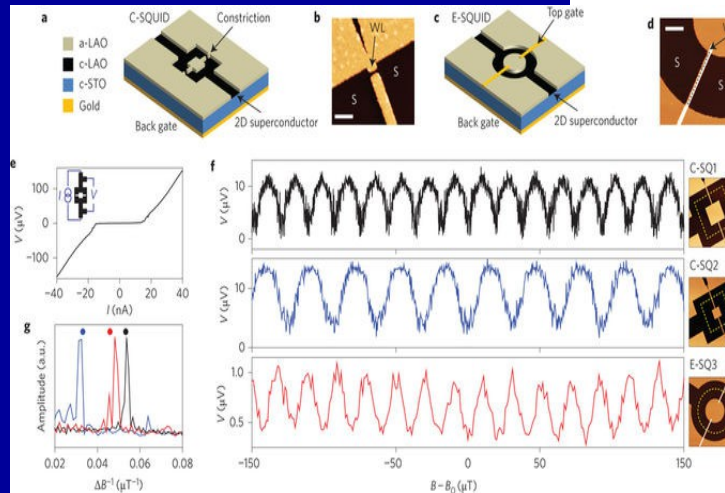
# My recent work

- Optomagnonics and magnon manipulation by light
- Non-linear nano- and optomechanics
- Nanostructures with complex oxides



Sanchar Sharma, Gerrit Bauer

Gary Steele Lab



Andrea Caviglia Lab

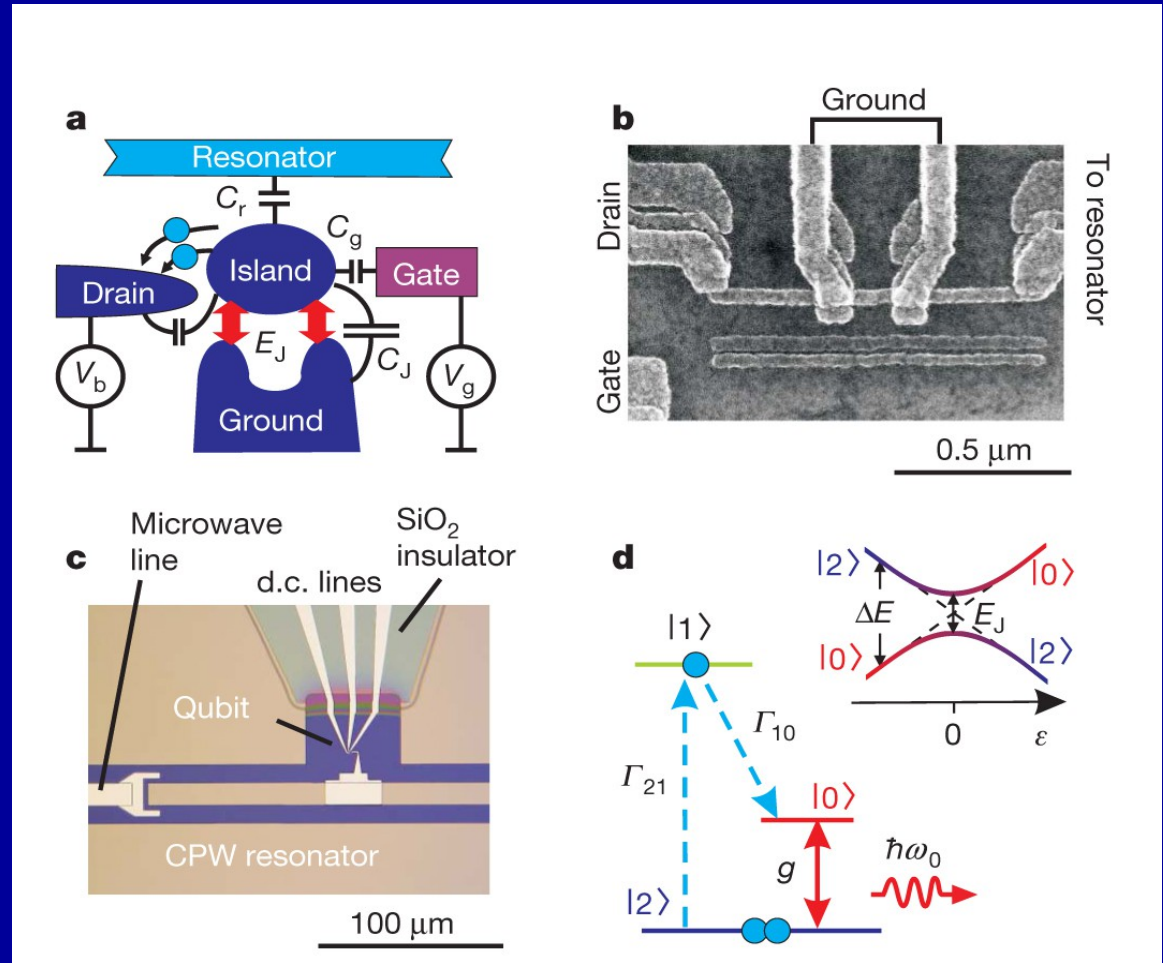
Yaroslav M. Blanter

Frank Hekking memorial workshop, January 2018

# Single artificial-atom lasing

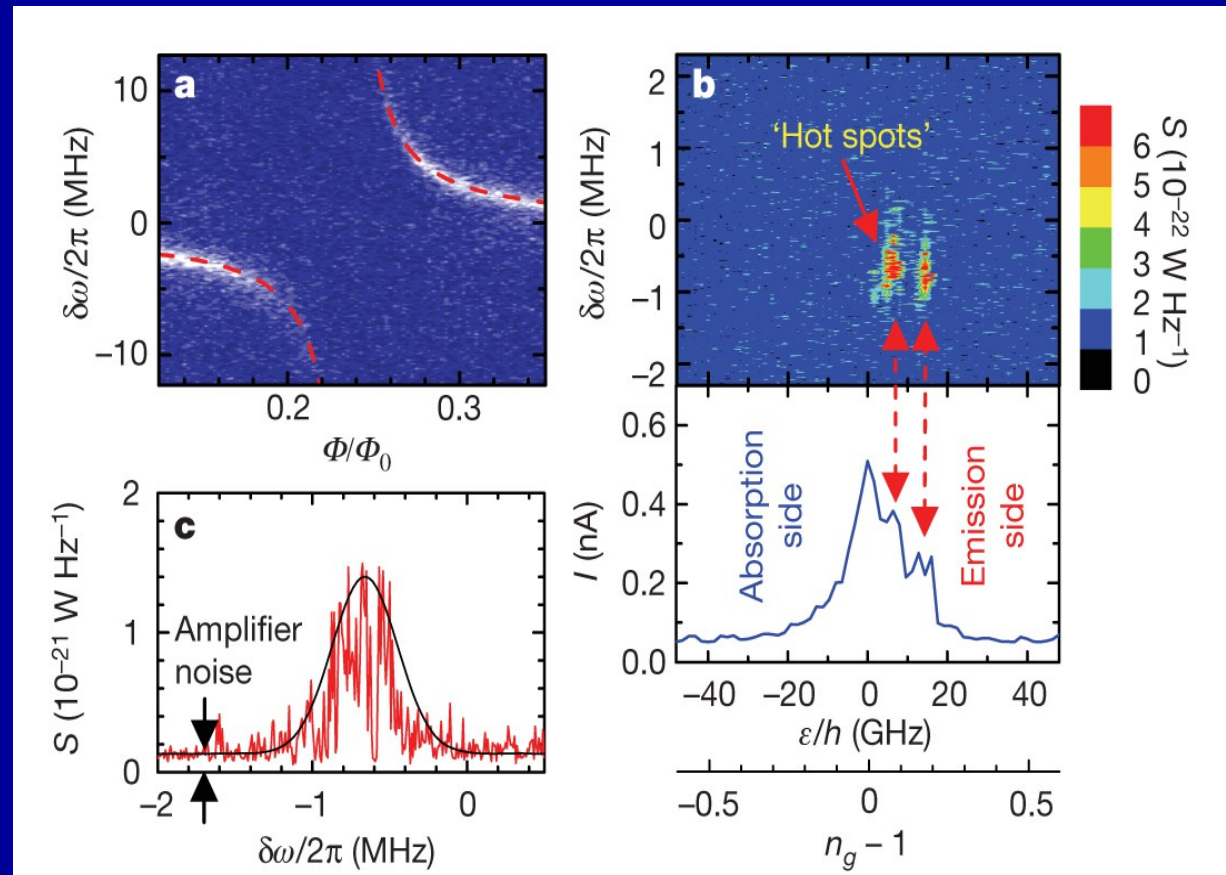
O. Astafiev, K. Inomata, A. O. Niskanen, T. Yamamoto, Yu. A. Pashkin, Y. Nakamura, and J. S. Tsai  
Nature **449**, 588 (2007)

Cooper pair box  
coupled to a  
microwave resonator



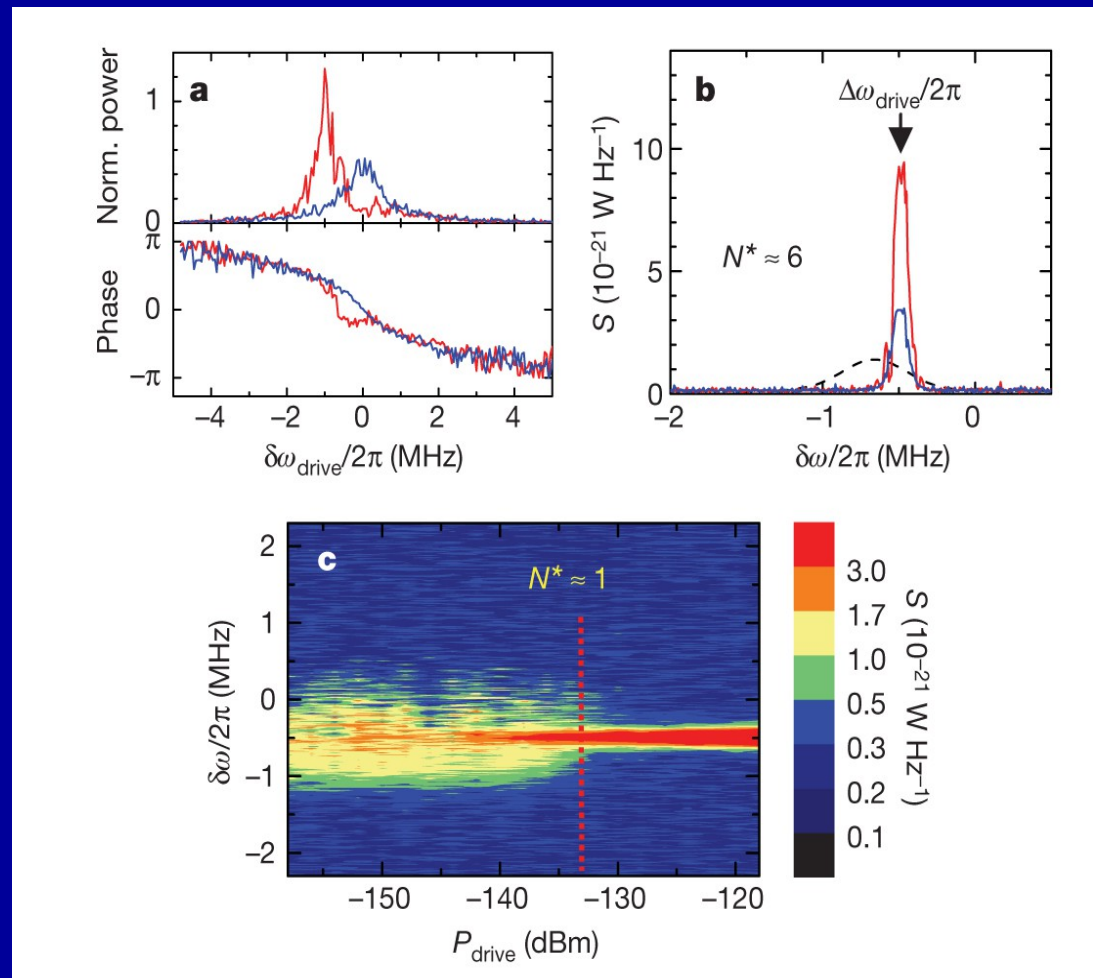
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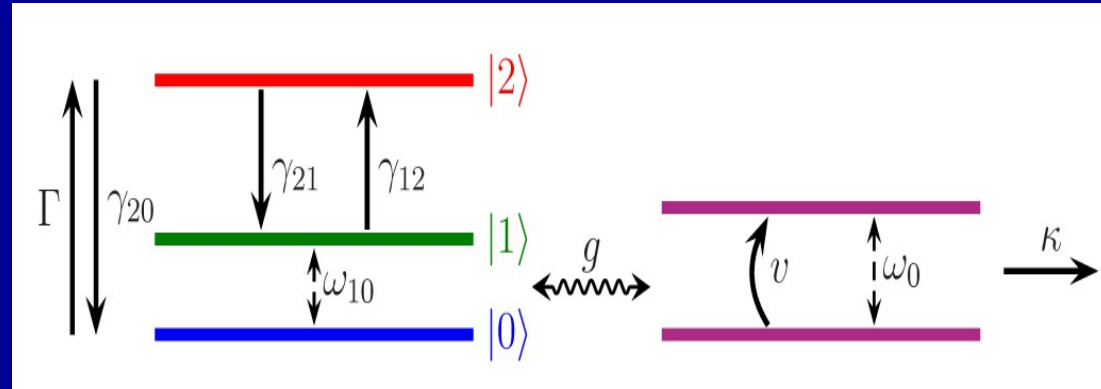
# Single artificial-atom lasing

## Theory:

S. André, V. Brosco, A. Shnirman, and G. Schön  
Phys. Rev. A **79**, 053848 (2009)

S. André, V. Brosco, M. Marthaler, A. Shnirman, and G. Schön  
Phys. Scr. T **79**, 014016 (2009)

# Hamiltonian

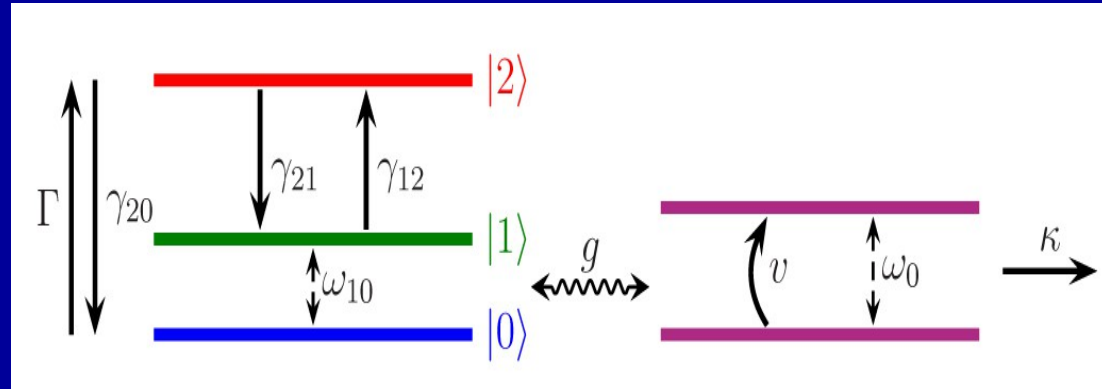


Jaynes-Cummings Hamiltonian:

$$H = \frac{1}{2} \hbar \omega_{10} \sigma_z + \hbar \omega_0 \hat{a}^\dagger \hat{a} + i \hbar g (\sigma_{01} \hat{a}^\dagger - \sigma_{10} \hat{a})$$

# Lindblad equation

$$\dot{\rho} = \frac{1}{i\hbar} [\hat{H}, \rho] + \hat{L}\rho$$

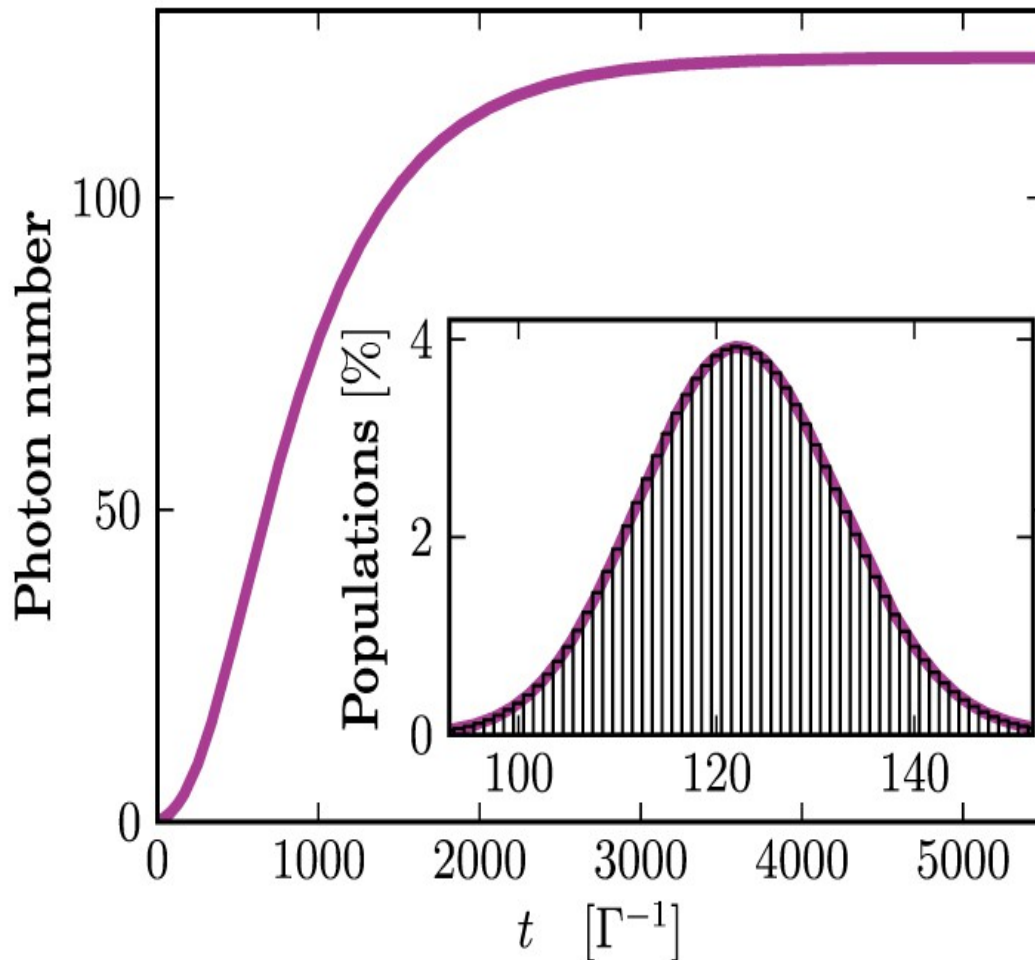


$$\hat{L} = \hat{L}_{\Gamma} + \hat{L}_{\gamma_{21}} + \hat{L}_{\gamma_{20}} + \hat{L}_{\gamma_{12}} + \hat{L}_{\kappa}$$

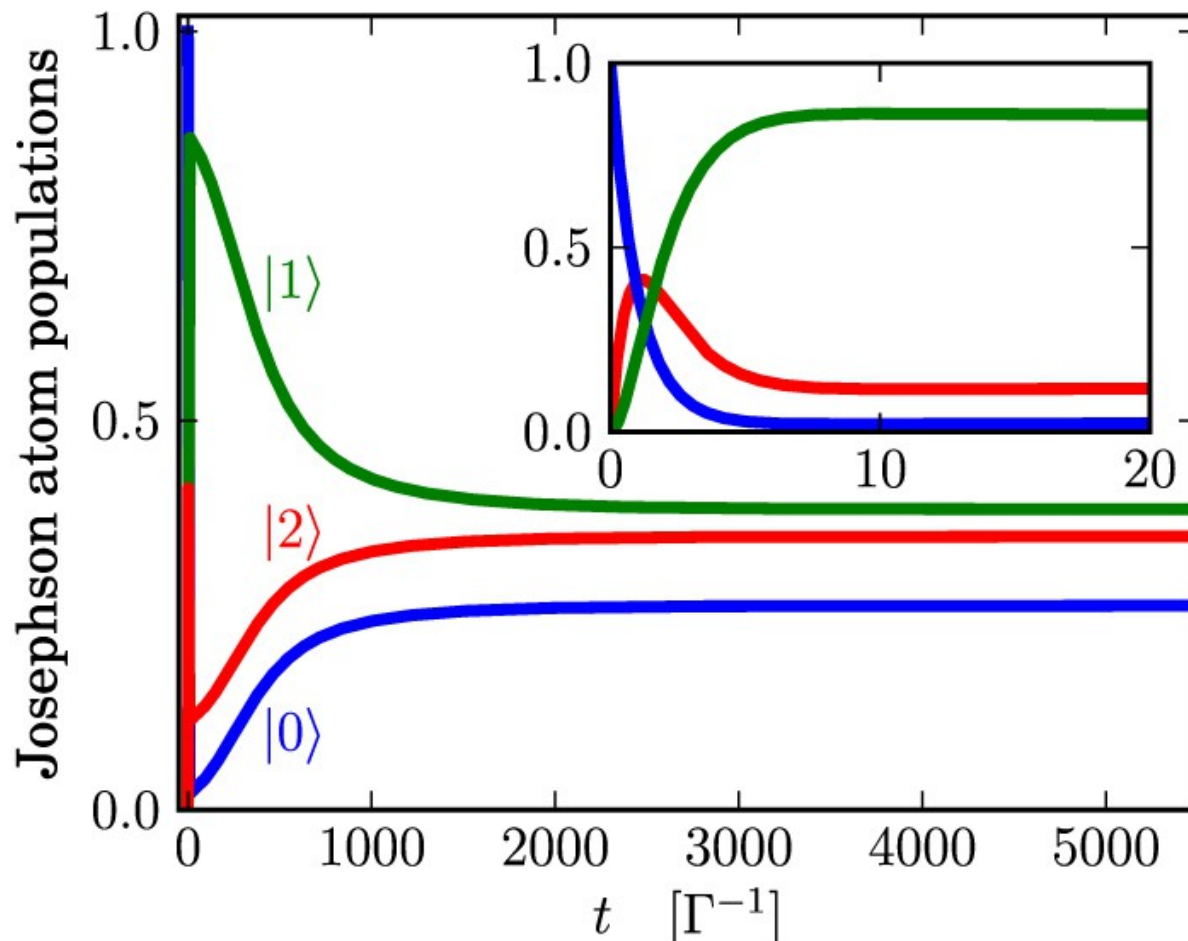
$$\hat{L}_{\gamma_{21}} = \frac{1}{2} \gamma_{21} (2\sigma_{21}\rho\sigma_{12} - \sigma_{11}\rho - \rho\sigma_{11}), \quad \sigma_{ij} = |i\rangle\langle j|$$

$$\hat{L}_{\kappa} = \frac{1}{2} \kappa (2\hat{a}\rho\hat{a}^{\dagger} - \hat{a}^{\dagger}\hat{a}\rho - \rho\hat{a}^{\dagger}\hat{a})$$

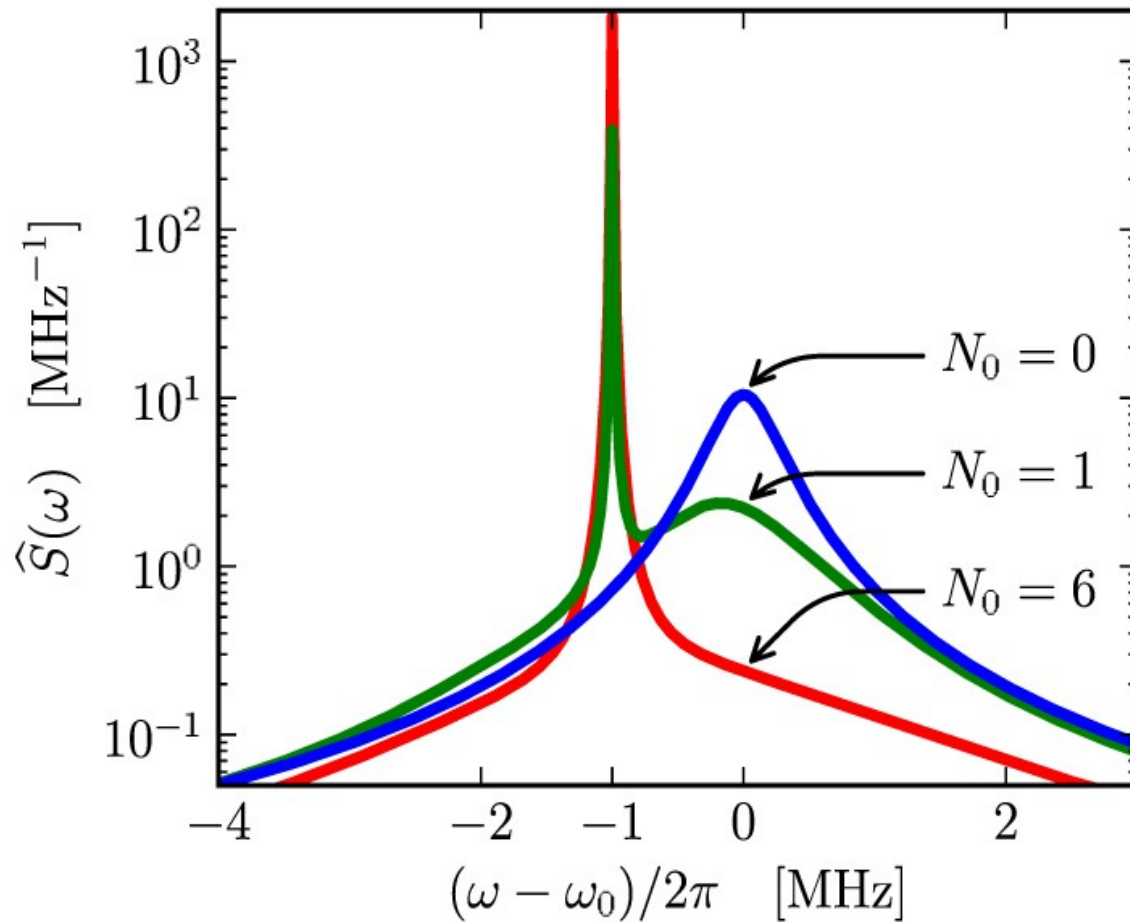
# Transient dynamics – Cavity



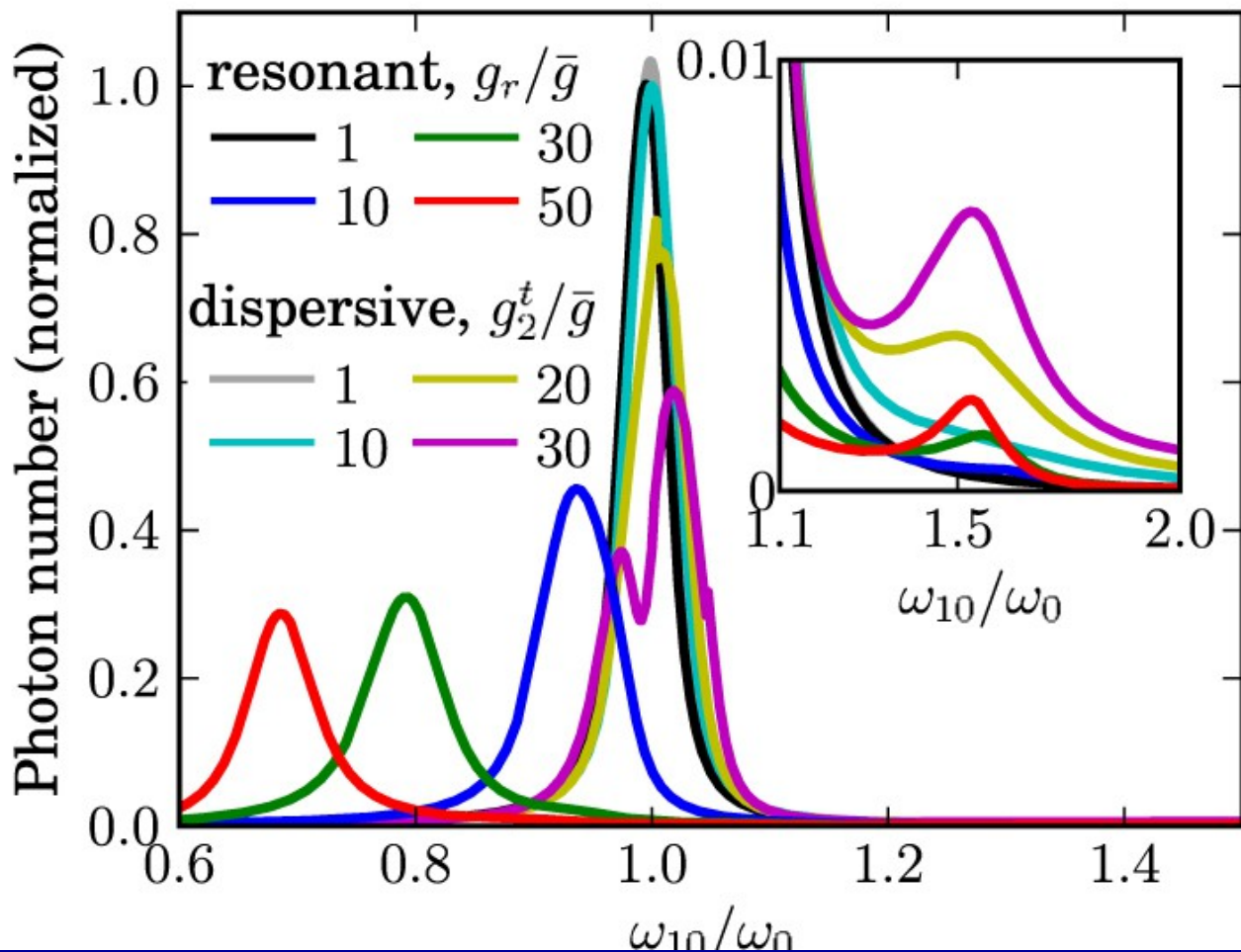
# Transient dynamics – Qubit



# Driven cavity

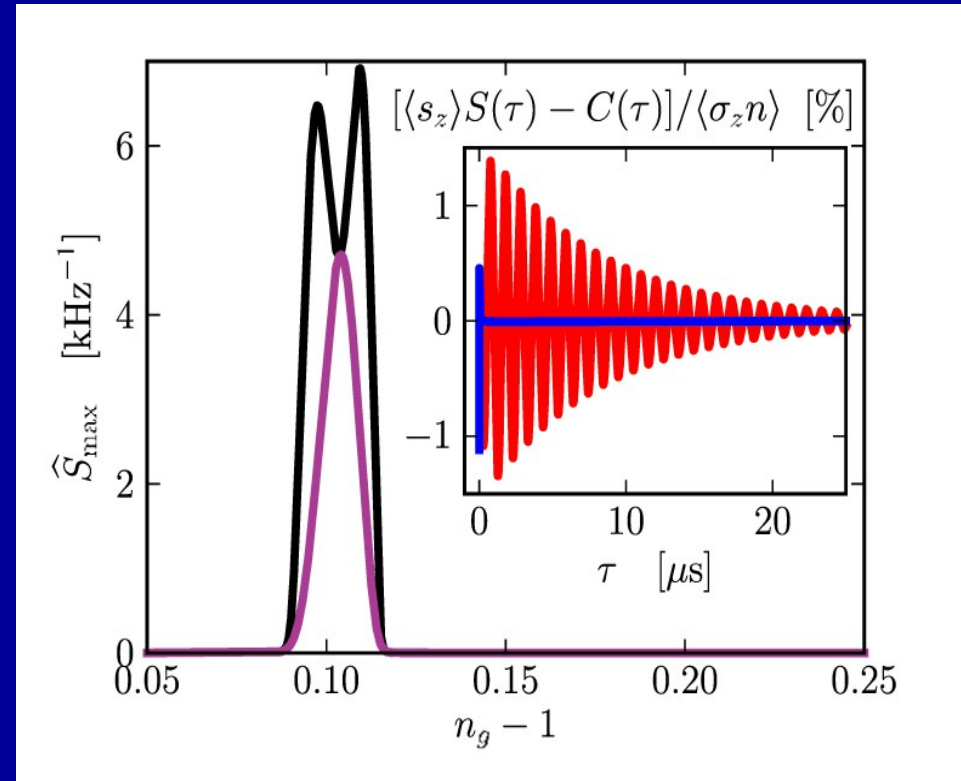


# Coupling to a two-level system



# Semi-classical approximation

$$\langle \sigma_z \hat{a}^\dagger \hat{a} \rangle \approx \langle \sigma_z \rangle \langle \hat{a}^\dagger \hat{a} \rangle$$



Fails close to the resonance



# Conclusions

- The Lindblad equation fully describes the dynamics of an artificial atom
- The additional peak can be due a coupling to a two-level system
- Semi-classical approximation fails close to the resonance